

Room-Temperature Magnetism of Ceria Nanocubes by Inductively Transferring Electrons to Ce Atoms from Nearby Oxygen Vacancy

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Abstract Ceria (CeO_2) nanocubes were synthesized by a hydrothermal method and weak ferromagnetism was observed in room temperature. After ultraviolet irradiation, the saturation magnetization was significantly enhanced from $\sim 3.18 \times 10^{-3}$ to $\sim 1.89 \times 10^{-2}$ emu g^{-1} . This is due to the increase of oxygen vacancies in CeO_2 structure which was confirmed by X-ray photoelectron spectra. The first-principle calculation with Vienna ab-initio simulation package was used to illustrate the enhanced ferromagnetism mechanism after calculating the density of states (DOSs) and partial density of states (PDOSs) of CeO_2 without and with different oxygen vacancies. It was found that the increase of oxygen vacancies will enlarge the PDOSs of Ce 4f orbital and DOSs. Two electrons in one oxygen vacancy are respectively excited to 4f orbital of two Ce atoms neighboring the vacancy, making these electron spin directions on 4f orbitals of these two Ce atoms parallel. This superexchange interaction leads to the formation of ferromagnetism in CeO_2 at room temperature. Our work indicates that ultraviolet irradiation is an effective method to enhance the magnetism of CeO_2 nanocube, and the first-principle calculation can understand well the enhanced magnetism.

Keywords UV irradiation · Oxygen vacancies · Saturation magnetism · Spin direction · Superexchange interaction

1 Introduction

Nanocrystalline ceria (CeO_2) has attracted much attention due to its fascinating mechanical and physic-chemical properties, as well as wide applications in various fields, including polishing materials [1, 2], automobile exhaust catalysts [3–5], fuel cell materials [6, 7], gas sensors [8, 9], high temperature superconducting materials [10], ultraviolet ray detectors, etc. [11, 12]. Recently, Zhang et al. [13] reported that CeO_2 nanoparticles have great potential for

multifunctional therapeutic applications in cancer therapy. Flytzani-Stephanopoulos et al. [14] used different nanostructured CeO_2 materials as a support to deposit gold clusters and found that Au/CeO_2 catalysts showed a strong support shape effect in the water-gas shift reaction. Most of the properties of cerium oxide was found to be related with oxygen vacancies in the structure [15–18].

It is well known that CeO_2 with perfect structure is paramagnetic. When one of oxygen atoms is removed, two electrons will be left and localized strongly at the f-level traps on two Ce atoms. This will cause the formal valence of two neighboring Ce atoms changing from +4 to +3, and therefore resulting in the formation of magnetism. Lee and co-workers [17] examined the localization behavior of CeO_2 with various degrees of oxygen deficiency as well as the associated magnetic properties and their origins using first-principles methods in the Vienna ab-initio simulation package (VASP). Choudhury and Choudhury [10] investigated how oxygen vacancies and cationic Ce^{3+} defects in ceria affect the band gap property by changing its structural

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regularity and then control its visible luminescence. In addition, vacancies in some other non-magnetic materials can also induce magnetism. Si et al. [19] found that vacancies in hexagonal boron nitride nanosheets (h-BN) could generate magnetic moments and form ferromagnetism, and they conducted some experiments to test their discovery.

Although some methods could generate magnetism change such as spin-reorientation transition (SRT) in ultrathin Ni films grown on Cu (100) [20], few papers report the experimental methods of obtaining oxygen vacancies and changing the valence state. Recently, Qin et al. [21] improved the magnetic properties of semiconductors and found that UV irradiation could significantly enhance the magnetism of the (111) twinned BaTiO₃ crystallites. They demonstrated that magnetism might originate from the increase in oxygen vacancies and Ti³⁺ cations formed by capturing an excited electron from Ti⁴⁺ under UV irradiation. Enlightened by this report, we speculate that the valence state might also change (from Ce⁴⁺ to Ce³⁺) under UV irradiation. Herein, the optical and magnetic properties of CeO₂ under UV irradiation were investigated and the electron density of states (DOSs) and the electron partial density of states (PDOSs) were calculated via density functional theory for a better understanding of the phenomenon.

2 Experimental Details

2.1 Synthesis of CeO₂ Nanocubes

The uniform organic-capping-free CeO₂ nanocubes were synthesized using a hydrothermal process [22]. Briefly, 434.3 mg of Ce(NO₃)₃·6H₂O and 1.6 mg of Na₃PO₄ were mixed in 40 mL deionized water and sonicated for 30 min. The mixed solution was then transferred into a Teflon-lined autoclave with 50 mL capacity. The vessel was sealed and heated at 200 °C for 24 h in an electric furnace. Then the product was collected and cleansed by centrifugation at 10,000 r min⁻¹ for 5 min and re-dispersed twice in ethanol. The precipitate was then calcined at 400 °C for 4 h and collected for further characterization.

2.2 UV Irradiation on CeO₂

The dried sample was uniformly distributed in a square crucible and put in a darkroom to irradiate for 24 h under the UV lamp.

2.3 Characterization of CeO₂

The powder X-ray diffraction (XRD) patterns were recorded on PANalytical Empyrean equipped with a PIXcel

with a 1D detector at 40 kV and 40 mA. Field emission scanning electron microscopy (FESEM) was carried out with a Nova 400 Nano microscope to analyze the morphology and size of the product. Transmission electron microscopy (TEM) was used to analyze the morphology and size of the samples with JEOL-400EX. The X-ray photoelectron spectra (XPS) were conducted by an ESCALab MKI X-ray photoelectron spectrometer, using non-monochromatized Mg K α X-ray as the excitation source. The reflection spectrum of the sample was measured using UV-3600 (SHIMADZU) UV-VIS-NIR Spectrophotometer. Magnetism measurement was carried out on superconducting quantum interference device (SQUIDS) measurement.

2.4 Computation of Magnetism

First-principles methods, implemented in the Vienna ab-initio simulation package (VASP) [23], were used to study the magnetism of CeO₂ without and with oxygen vacancies. Because of the strong Coulomb interaction of the localized Ce 4f electrons, the standard density functional theory (DFT) calculations with the correction of Hubbard *U* parameter (DFT+*U*) were employed [24, 25]. We chose *U* = 7 eV [26] to improve the prediction of the computation. And a 500 eV plane-wave energy cutoff was used to expand the electronic wave functions. The 7 × 7 × 7 Monkhorst–Pack grid was used for the sampling of the Brillouin zone during geometrical optimization. A supercell of 2 × 2 × 2 without any vacancy and with different oxygen vacancies was built to simulate the magnetic properties of CeO₂. All the atomic positions and lattice parameters were relaxed and optimized until the convergence of force reaches 0.01 eV Å⁻¹.

3 Results and Discussion

A typical XRD pattern of the sample is shown in Fig. 1a. All the peaks can be indexed to the cubic phase (Fm3m, JCPDS 34-0394) of CeO₂ without any impurity peaks. FESEM images of the synthesized CeO₂ sample, as shown in Fig. 1b, c, demonstrate that the particles are quite uniform and have regular cube-like morphology with a size of 200 nm. TEM image in Fig. 1d also shows clear cubic shape of CeO₂ particle. The inset is the high-resolution TEM image of the selected area, which has lattice planes (100) with *d*-spacing of 0.27 nm.

Figure 2a, b show UV-Vis reflectance spectra and Kubelka–Munk functions of the CeO₂ nanocubes without and with UV irradiation. Extrapolating the linear part of Kubelka–Munk function, which is actually the ratio of the absorption and scattering factors from the optical diffuse

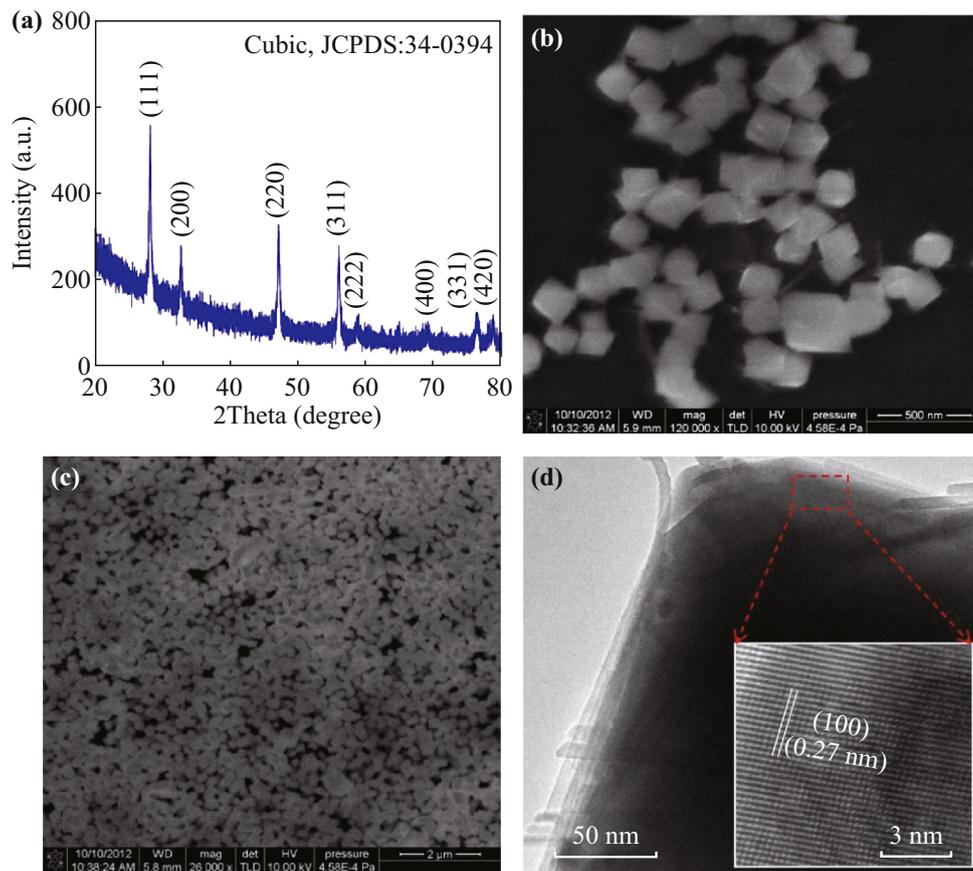


Fig. 1 a XRD, b, c FESEM images, and d TEM image of the CeO₂ sample

reflectance spectrum [27], the energy gap of the CeO₂ can be evaluated as 3.13 and 3.04 eV for the CeO₂ sample without and with UV irradiation, respectively (Fig. 2a, b) [28, 29]. The reduced band gap can be attributed to the defect energy level, as some previous studies have reported that oxygen deficiencies create additional energy level within the forbidden energy gap [30, 31].

Since the intensity of Ce 4p and Ce 4d is much lower compared to that of Ce 3d, we choose Ce 3d signal in XPS results to analyze further. Figure 3a shows the photoelectron spectrum of Ce 3d core level before UV irradiation, among which V and U are for Ce³⁺ and Ce⁴⁺ states, respectively. The binding energy peaks labeled as V1 and V2 are located at 883.26 eV and 902.81 eV, indicating the Ce³⁺3d_{5/2} and Ce³⁺3d_{3/2}. The peaks (U1, U2, U3, U4, U5, and U6) of Ce⁴⁺3d_{5/2} and Ce⁴⁺3d_{3/2} are respectively shown at binding energy of 881.48, 888.34, 897.73, 899.85, 907.05, and 916.34 eV [32–34]. Compared with the sample after UV irradiation in Fig. 3b, it can be found that positions of Ce 3d peaks are nearly unchanged. However, the content of elements changes and the intensity ratio of Ce³⁺ to Ce⁴⁺ increases from 0.260 to 0.332. This may be ascribed to the increase of Ce³⁺ ions after UV irradiation.

Figure 3c shows the O 2p core level of the sample before UV irradiation, labeled as O1, O2, and O3, which indicates the valence of O is -2. The levels of O 2p peaks at 528.83 and 530.86 eV are ascribed to O²⁻ ions which are related to Ce⁴⁺ and Ce³⁺ ions [33], while the peak of 532.47 eV is attributed to the oxygen absorbed onto the surface of the samples [35, 36]. Same with Ce 3d, the positions of O 2p peaks after UV irradiation do not shift while the relative intensity of these peaks changes (Fig. 3d), which indicates the change of element quantity. In calculation results, the intensity ratio of O2 to O1 increases from 1.183 to 1.291, demonstrating that the O²⁻ ions related to Ce³⁺ increase, which confirms the increase in oxygen vacancies. All the curve-fitting processes in Fig. 3 use a mixed Gaussian–Lorentzian simulation method with the same full width at half-maximum.

Figure 4 shows the hysteresis loops of sample from -15,000 Oe to +15,000 Oe before and after UV irradiation. The saturation magnetization of the sample before UV irradiation is 3.18×10^{-3} emu g⁻¹, while it was greatly enhanced to 1.89×10^{-2} emu g⁻¹ after UV irradiation. This may relate to the increase of oxygen vacancies caused by UV irradiation.

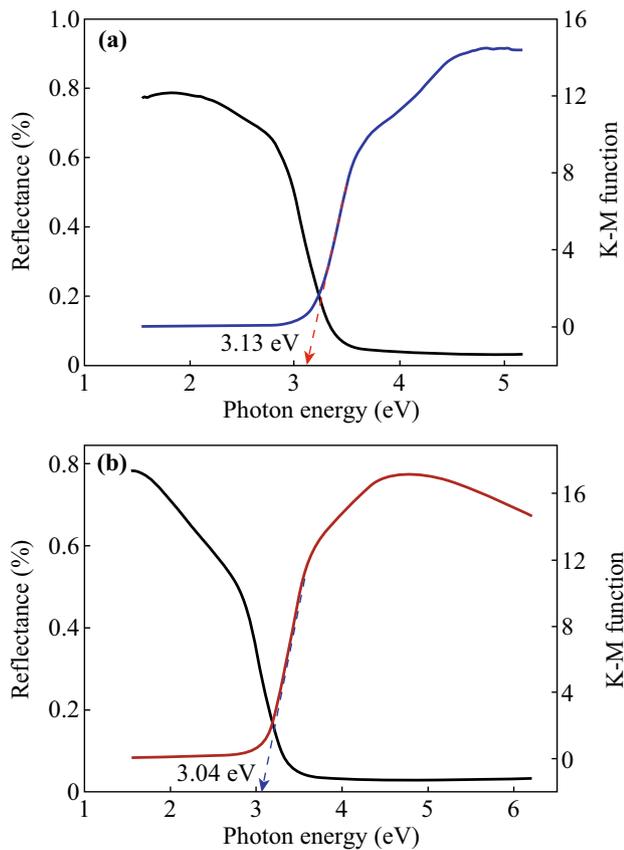


Fig. 2 UV-Visible reflectance spectrum and Kubelka-Munk function of the CeO_2 sample before (a) and after (b) UV irradiation

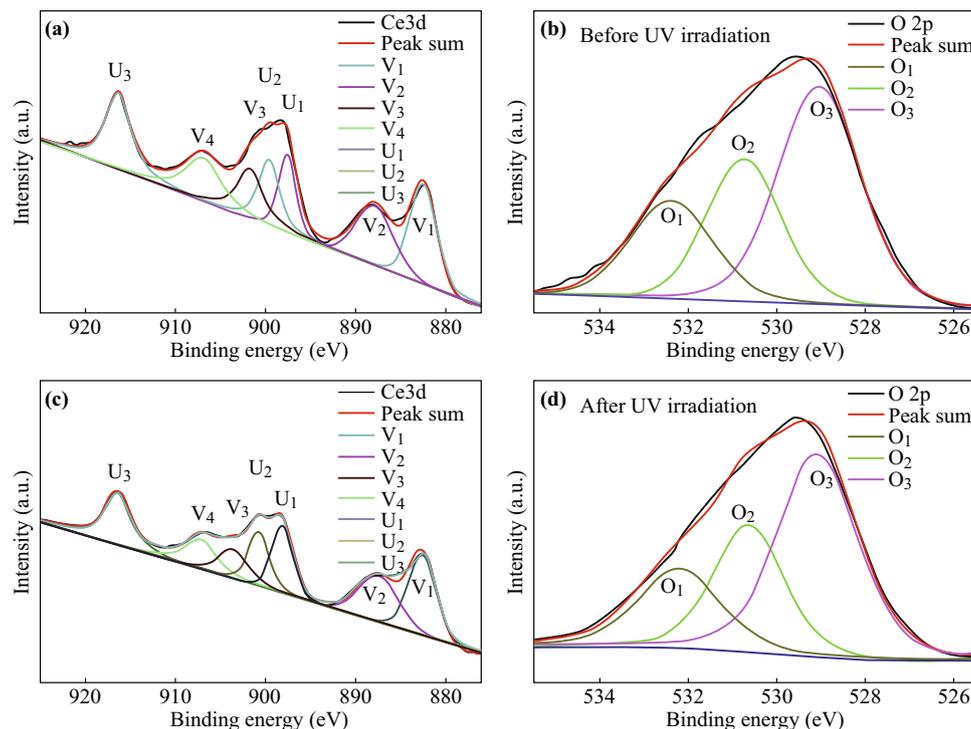


Fig. 3 a Ce 3d core level, and b O 2p core level for the CeO_2 sample before UV irradiation. c Ce 3d core level, and d O 2p core level for the CeO_2 sample after UV irradiation

From the above discussion, we have demonstrated that UV irradiation can generate oxygen vacancies, and oxygen vacancies will induce the enhancement of magnetism. In order to understand the mechanism, electron DOS, projected density of states (PDOS), and the magnetism of the structure were calculated using the first-principle calculation in the VASP. In all calculations, the projector augmented wave method (PAW) [37] with the frozen-core approximation was used for the ion-electron interactions. Exchange correlation interactions were described by the generalized gradient approximation (GGA) [38].

The DOSs and PDOSs of CeO_2 without and with one oxygen vacancy and two oxygen vacancies were calculated and the results are shown in Fig. 5. One can see the perfect structure of tetrahedral CeO_2 supercell with 32 cerium atoms and 64 oxygen atoms. Each oxygen atom is surrounded by four cerium atoms with the same distance. To simplify the atom orbitals, the f orbitals of Ce 4f are marked as $4f_{-3} \sim 4f_3$ and the p orbitals of O 2p are marked as $P_x \sim P_z$ as shown in Fig. 5b. From the total DOS of CeO_2 , all the electron spin-up and spin-down states are symmetric and show no magnetism in the perfect CeO_2 cell. Comparing the Ce 4f state with O 2p, we have observed that O 2p contributes more to the total DOS at the top valence band than the Ce 4f. While at the bottom conduction band the majority was formed by Ce 4f. The integrative action of Ce 4f and O 2p makes the CeO_2 non-magnetic. When one oxygen is removed, an oxygen

vacancy is generated, as shown in Fig. 5c. Several PDOSs of Ce 4f are symmetric except f-3, f-2, and f3, which generate most of the magnetism of CeO₂ with one vacancy. From the PDOSs of O 2p, the P_x, P_y, and P_z states are symmetric at the top valence band constituting most of the valence band of CeO₂, as can be seen from Fig. 5d. Meanwhile, at the bottom conduction band, O 2p exhibits slight asymmetry which contributes to the formation of the conduction band of CeO₂. With one oxygen vacancy, the calculation of magnetism of the sample is about 1.213 μB. After another oxygen atom is removed, two oxygen vacancies are formed. Herein, we choose two cases to analyze the magnetism as depicted in Fig. 5e, g. Comparing the DOSs and PDOSs of Ce 4f and O 2p in Fig. 5f, h, it is not difficult for us to discover that all their electron spin-

up and spin-down in f orbitals of Ce 4f are asymmetric, generating most of the magnetism of CeO₂. Same as the situation in Fig. 5b, the electron spin-up and spin-down of O 2p are symmetric at the top valence band and reveal a bit of asymmetry at the bottom conduction band. Since the asymmetry of PDOSs in f orbitals in Fig. 5h is higher than that of PDOSs in f orbitals in Fig. 5f, the magnetization of the sample in Fig. 5h is larger than that in Fig. 5f in accordance with the values in the figure ($M_2 = 1.912 \mu\text{B}$, $M_{2'} = 1.968 \mu\text{B}$). Moreover, the magnetization of the sample with two oxygen vacancies is obviously larger than that with one oxygen vacancy, which well matches our demonstration that the enhancement of the magnetism of CeO₂ after UV irradiation is due to the generation of oxygen vacancies. Since the oxygen vacancy exhibits positive electricity, it attracts nearest oxygen atoms. The blue arrows in Fig. 5c, e, g demonstrate the displacement of the neighboring oxygen atoms. All the structures of CeO₂ without and with oxygen vacancies are optimized in the calculations of the DOSs, PDOSs, and magnetism.

Figure 6a shows the schematic of superexchange interaction among 1Ce, 2Ce, and O atoms. The two Ce atoms are respectively reduced by two electrons from the oxygen vacancy, forming a Ce–O–Ce bond together with the neighboring O atom, which favors a 90° superexchange interaction, leading to magnetism [17, 39]. Figure 6b–f display the process of superexchange interaction of Ce–O–Ce. First, one electron on one O 2p orbital is excited by UV irradiation to one 4f orbital of 1Ce atom (Fig. 6c), and its spin direction is parallel to the electron on Ce 4f orbital based on Hund’s rule [40] (Fig. 6d). Since the Ce–O–Ce bond angle is close to 90°, the electron with the same spin

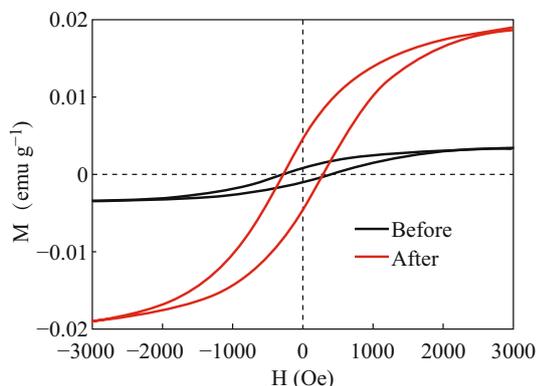


Fig. 4 Hysteresis loops of the CeO₂ sample before and after UV irradiation measured at room temperature

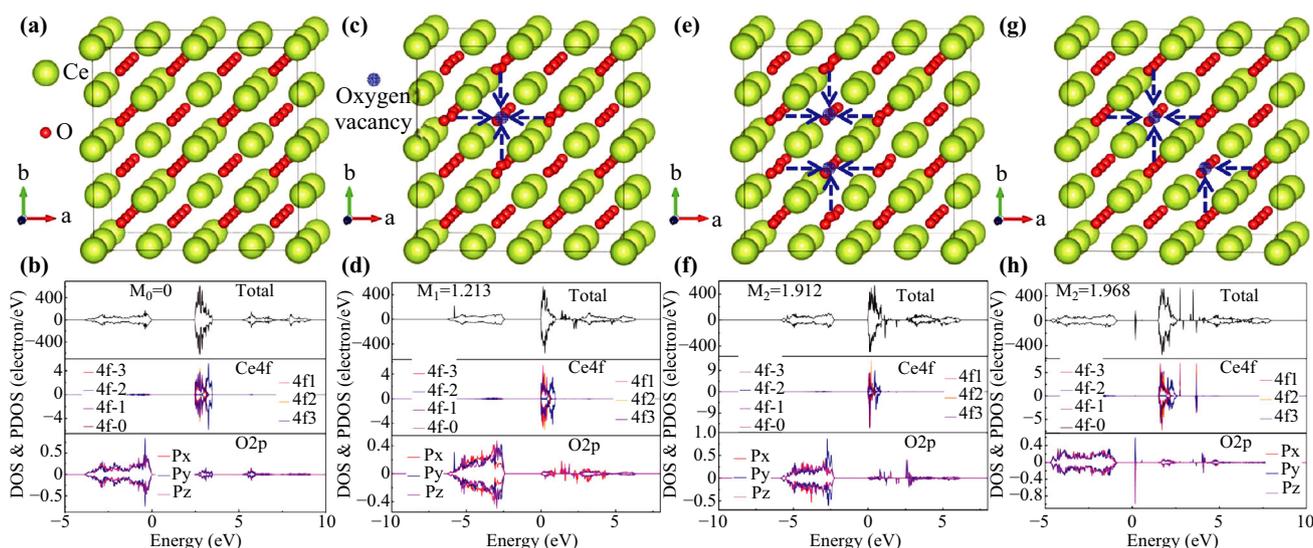


Fig. 5 The schematic of CeO₂ supercell without any oxygen vacancy (a), with one oxygen vacancy (c), two oxygen vacancies (e, g), and their corresponding DOSs and PDOSs (b, d, f, and h)

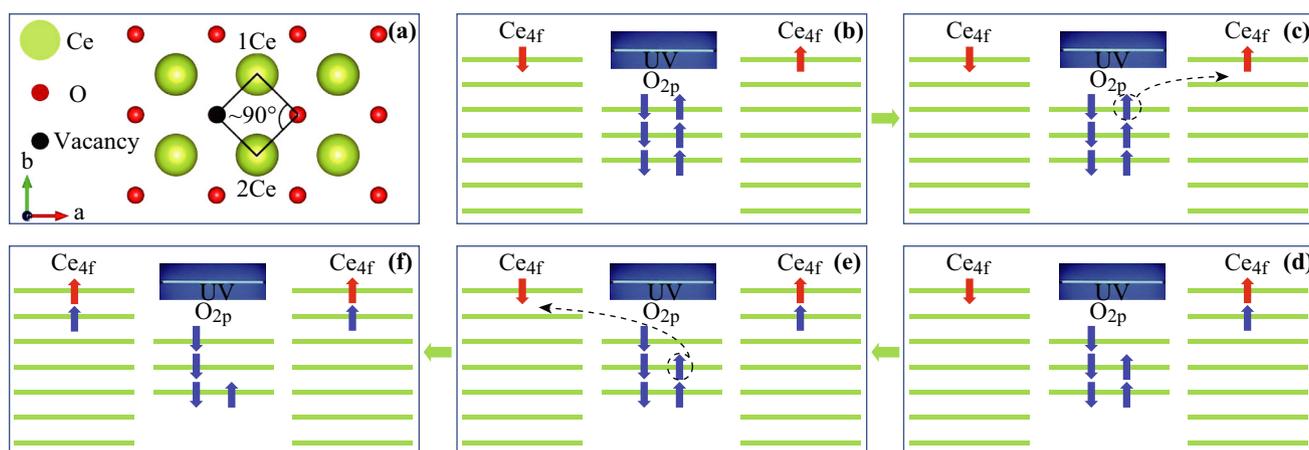


Fig. 6 The schematic of superexchange interaction among 1Ce, 2Ce, and O (a), and the process of superexchange interaction of Ce–O–Ce (b–f)

direction on another O 2p orbital is exchanged with 4f orbital of 2Ce atom (Fig. 6e), which makes the spin direction of the electron on 2Ce 4f orbital parallel to it (Fig. 6f). Therefore, the magnetic moments of these two Ce atoms have the same direction, generating ferromagnetic coupling. With the increase in oxygen vacancies, the tetrahedral structure of the sample is further destroyed, making the Ce atoms close to the oxygen vacancies, which increases the total magnetic momentum. Back to Fig. 5, as UV irradiation produces more oxygen vacancies in the structure of CeO₂, the electron spin on Ce 4f orbitals becomes more complicated, making the PDOSs of Ce 4f more asymmetric. Thus UV irradiation can enhance the magnetism by producing oxygen vacancies.

4 Conclusions

In this work, uniform CeO₂ nanocubes were synthesized and oxygen vacancy can be increased and therefore the magnetism was enhanced by UV irradiation. The first-principle calculation was used to explain the magnetism enhancement mechanism. According to the calculation results, the increase of oxygen vacancy which confirmed by XPS measurements will enhance the DOSs of Ce4f orbital, and therefore superexchange interaction of Ce–O–Ce generates magnetism. This work demonstrates an effective route to produce diluted magnetism for CeO₂ nanocubes and offers a better understanding of room-temperature magnetism in CeO₂ nanocrystals.

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